

Solid Rocket Motors

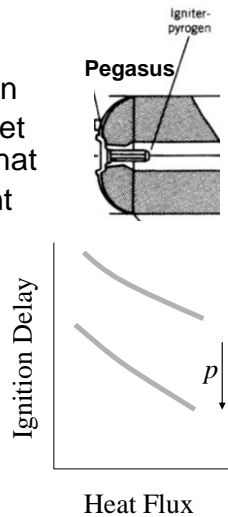
Transients and Combustion Instability

Solid Motor Unsteady Combustion

- Two parts of motor firing are by definition transient phenomena
 - ignition
 - extinction/termination
- Can also have unsteady combustion during what should be nominally steady operation
 - combustion instability

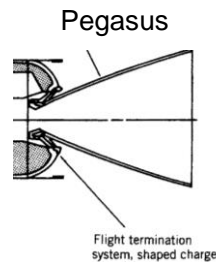
Ignition

- Goal is obviously successful ignition
 - pyrotechnics/pyrogens most common
- Need sufficiently large heat source to get enough of the propellant to burn such that
 - heat losses to surrounding propellant does not extinguish flame
 - motor pressure continues to sustainable level
 - recall poor burning at low pressure
- Additional goal may be shorter ignition delay
 - requires even greater ignition energy



Extinction/Termination

- Motor will burn itself out when
 - no propellant left
 - amount of propellant (surface area) remaining is insufficient to keep pressure at sustainable level
- Motor can extinguish if sudden depressurization (dp/dt)
 - flame suddenly lifts farther from surface; remaining thermal energy in surface produces too much for flame to consume nearby and heat feedback too low
- Depressurization can be caused by
 - sudden increase in nozzle throat size
 - sudden “opening” of new exhaust path



Combustion Instability

- Like liquid rockets
 - solid motors can experience unsteady operation due to feedback between motor conditions and propellant burning (dq/dt and dp/dt)
 - Unlike liquid rockets
 - no separate propellant feed system
 - no spray/atomization
 - combustion feedback not localized to head end
 - combustion occurs along full length for port burning
 - chamber volume (and cross-section) not constant
 - chamber lined by acoustically dissipative, compressible material
- excellent reference: *Nonsteady Burning and Combustion Instability of Solid Propellants*, Vol. 143, *Progress in Astro. and Aero.*, ed., De Luca, Price and Summerfield

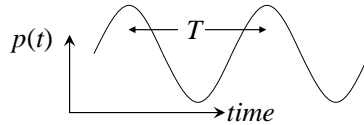
Types of Combustion Instability

- Low frequency
 - “non-acoustic”
 - spatially uniform pressure oscillations
 - ~5-300 Hz
- Intermediate frequency
 - longitudinal acoustic modes of motor
 - ~15-1500 Hz
- High frequency
 - transverse acoustic modes of motor
 - ~1000-15,000 Hz

Characteristic Times

- Instability period

– $T = 1/f$



- Residence (flushing) time of motor chamber

– $t_{res} = m/\dot{m} = \rho_o V_o / \dot{m}$

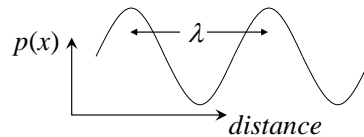
- Relaxation time of propellant combustion wave

– can be due to thermal wave in condensed phase of propellant (t_{th})

– gas flame response (t_{fl})

- Also can describe wavelength (λ) of oscillation in motor

$\lambda = a / f$



Low-Frequency Instability

- Spatially uniform pressure oscillations

– essentially Helmholtz resonator

- Attributable when $T/t_{res} > 1$

- Also called

– chuffing/chugging

– bulk mode

– L^* (sometimes occurs when $L^* = V_o/A_t$ too low)

- lowest L^* during initial portion of burn

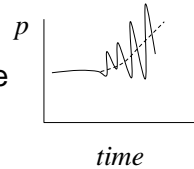
- Primarily driven by response of propellant combustion to pressure oscillation

- Can be addressed analytically to reasonable degree

– occurs for $t_{res}/t_{th} (\equiv Da) \sim 0.2$

High Frequency Instability

- Transverse modes
 - $\lambda \sim 2D$ (“characteristic” lateral dimension of internal volume) and harmonics
 - $f \sim a/2D$
 - D not constant \Rightarrow resonant frequency(s) evolve
- If oscillations grow, mean burning rate also increases
 - rapid rise in transient & mean pressure (and thus thrust)
 - can lead to catastrophic failures (many early motors)
- Thought to be driven primarily by response of propellant combustion to pressure oscillations (as opposed to “velocity-coupling”)



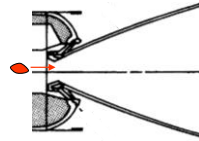
High Frequency - Damping

- Growth and maximum amplitude of oscillations controlled by feedback vs. damping
- Various damping sources
 - radiation out of nozzle (typically low level damping)
 - drag of condensed phase material in flow
 - e.g., Al_2O_3
 - depends on particle loading and size distribution (frequency dependence)
 - viscous/turbulent/vortical dissipation of acoustic energy
- **Control approaches:** particle size/loading (Al or inerts); port cross-section; rods and baffles



Intermediate Frequency Instability

- Longitudinal modes
 - $\lambda \sim L$
 - modes do not change much with time (but which modes have energy can)
- Can produce large increase in mean burning rate when oscillation is large
- Can be triggered by flow disturbances
 - slivers, vortex shedding, ...
- Damping
 - low enough f that particle damping small
 - nozzle damping higher
- Main flow and acoustic wave co-linear
 - “velocity-coupling” more important than with transverse modes



Instability Modeling

- Analysis and characterization of instabilities for design purposes often broken into
 - (non-reacting) acoustic problem
 - combustion response function (assumes feedback based on near surface processes)
 - coupled by interface condition (acoustic admittance)
- Velocity coupling requires more sophisticated approaches
 - one example is jet/vortex shedding from slots between segments in large segmented motors

Measuring Combustion Response Function

- Measured for propellants in simplified burner
- One standard approach is the “T-burner”
 - center vented, symmetric
 - frequencies determined by (changing) length
 - low Mach number near propellant to minimize mean flow velocity effects
 - analytic model of T-burner used to determine combustion response function (f, T, p, \dots)

